

Calculus I SI Worksheet

Section 3.3 Trig Derivatives

$$\frac{d}{dx} \sin(x) = \cos(x)$$

$$\frac{d}{dx} \csc(x) = -\csc(x) \cot(x)$$

$$\frac{d}{dx} \cos(x) = -\sin(x)$$

$$\frac{d}{dx} \sec(x) = \sec(x) \tan(x)$$

$$\frac{d}{dx} \tan(x) = \sec^2(x)$$

$$\frac{d}{dx} \cot(x) = -\csc^2(x)$$

1. $\frac{d}{dx} \sin(x) + x^2 \tan(x) + 3$

$$\frac{dy}{dx} = \cos x + 2x \tan x + x^2 \sec^2 x$$

$$\begin{array}{r|l} x^2 & \tan(x) \\ \hline 2x & \sec^2(x) \end{array}$$

2. $\frac{d}{dx} \cos(x) \sin(x) + \frac{1}{3} x^3$

$$\frac{dy}{dx} = -\sin^2 x + \cos^2 x + x^2$$

$$\begin{array}{r|l} \cos x & \sin x \\ \hline -\sin x & \cos x \end{array}$$

3. $\frac{d}{dx} \frac{\sin(x)+1}{\cos(x)}$

$\sin x + 1$	$\cos x$
$\cos x$	$-\sin x$

$$\frac{dy}{dx} = \frac{\cos^2 x + \sin^2 x + \sin x}{\cos^2 x}$$

* $\cos^2 x + \sin^2 x = 1$

$$\frac{dy}{dx} = \frac{1 + \sin x}{\cos^2 x} = \sec^2(x) + \sec x \tan x$$

OR

$$\frac{\sin x + 1}{\cos x} = \frac{\sin x}{\cos x} + \frac{1}{\cos x} = \tan x + \sec x$$

$$\frac{dy}{dx} = \sec^2 x + \sec x \tan x$$

4. $\frac{d}{dx} x^2 - \sin(x) \csc(x)$

$$\frac{dy}{dx} = 2x - \csc x \cos x + \sin x \csc x \cot x$$

$\swarrow \quad \searrow \quad \swarrow \quad \searrow$
 $\frac{1}{\sin} \quad \frac{\cos}{\sin} = \cot \quad \frac{1}{\sin}$

$\sin x$	$\csc x$
$\cos x$	$-\csc x \cot x$

$$\frac{dy}{dx} = 2x - \cot x + \cot x$$

$$\frac{dy}{dx} = 2x$$

OR

$$-\sin x \csc x = -\sin x \frac{1}{\sin x} = -1$$

$$\frac{d}{dx} (x^2 - 1)$$

$$\frac{dy}{dx} = 2x$$